

2_1: Solving Systems with $y = mx + b$

Remember the \$600 raised by selling shirts and caps? It is *ba-a-a-ck!*



How can you find the number of shirts and number of caps sold?

Nyla and Jimfa both write a system of two linear equations.

$$\begin{cases} c + s = 18 \\ 10c + 5s = 125 \end{cases}$$

Nyla and Jimfa both rewrite each equation in slope-intercept form, equivalent equations.

$$\begin{cases} c = -s + 18 \\ c = -0.5s + 12.5 \end{cases}$$

Nyla graphs the two equations. The solution is the intersection point.

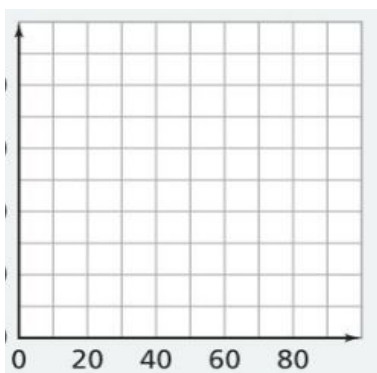
Jimfa sets the two expressions for c equal, then solves for a single variable s .

$$-0.5s + 12.5 = -s + 18$$

A

- Solve the system using Nyla's method. (BE SURE to label the SCALE, and identify which axis is c and which axis is s .)

$$\begin{cases} c = -s + 18 \\ c = -0.5s + 12.5 \end{cases}$$



Solve the system using Jimfa's method. (Jimfa's method is **symbolic**; he uses symbols only, not a graph, to solve.)

$$-0.5s + 12.5 = -s + 18$$

Solve the linear equation for s .
Then find the related value of c .

How many shirts and caps did the class sell? Explain your reasoning.

In part B, use Jimfa's method; do NOT graph.

B Use symbolic methods to find values of x and y that satisfy each system. Check your solution by substituting the values into the equations and showing that the resulting statements are true.

1.
$$\begin{cases} y = 1.5x - 0.4 \\ y = 0.3x + 5 \end{cases}$$

2.
$$\begin{cases} x + y = 3 \\ x - y = -5 \end{cases}$$

3.
$$\begin{cases} 3x - y = 30 \\ x + y = 14 \end{cases}$$

4.
$$\begin{cases} x + 6y = 15 \\ -x + 4y = 5 \end{cases}$$

5.
$$\begin{cases} x - y = -5 \\ -2x + 2y = 10 \end{cases}$$

6.
$$\begin{cases} x - y = -5 \\ -2x + 2y = 8 \end{cases}$$